

What is claimed is:

1. A method of generating a reconstructed 2D image of a 3D scan volume  $f(x,y,z)$  of an object, for an orientation  $(\theta, \phi, \varphi)$  of the 3D scan volume  $f(x,y,z)$ , the method comprising:
  - a. generating 3D scan data representative of the 3D scan volume  $f(x,y,z)$  of said object;
  - b. computing a 3D Fourier transform  $F(u,v,w)$  of the 3D scan volume  $f(x,y,z)$ , wherein  $u,v$ , and  $w$  are variables in a three-dimensional frequency domain;
  - c. sampling a surface  $S(\theta, \phi, \varphi, u', v')$  within said 3D Fourier transform  $F(u,v,w)$ , at angles  $(\theta, \phi, \varphi)$  corresponding to said orientation of said 3D scan volume; and
  - d. computing the 2D inverse Fourier transform  $F^{-1}[S(\theta, \phi, \varphi, u', v')]$  of said surface  $S(\theta, \phi, \varphi, u', v')$ .
2. A method in accordance with claim 1, wherein the reconstructed 2D image comprises a DRR (digitally reconstructed radiograph).
3. A method in accordance with claim 2, wherein  $F^{-1}[S(\theta, \phi, \varphi, u', v')]$  is a 2D DRR reconstructed along a projection direction perpendicular to said surface  $S(\theta, \phi, \varphi, u', v')$ .
4. A method in accordance with claim 3,
  - wherein the projection direction comprises a direction of a cone projection, the cone projection being the projection of a beam originating from a point source, passing through the scan volume, and incident upon a planar 2D surface;
  - wherein said 2D DRR represents the radiographic image of the scan volume that would be obtained with an imaging beam emitted from a point source disposed at a known position and angle, if said scan volume were positioned in accordance with said 3D scan data; and

wherein the step of sampling said surface  $S(\theta, \phi, \varphi, u', v')$  within said Fourier transform  $F(u,v,w)$  comprises the step of selecting the sampling surface in a way that the sampled surface is part of the surface of a sphere whose center is coincident with said point source.

5. A method in accordance with claim 1, wherein said 3D scan data comprise at least one of: CT scan data, PET (positron emission tomography) scan data, MRI (magnetic resonance imaging) scan data, and ultrasound scan data.

6. A method in accordance with claim 1, wherein sampling in part c said surface  $S(\theta, \phi, \varphi, u', v')$  at angles  $(\theta, \phi, \varphi)$  comprises selecting a 3D resampling kernel.

7. A method in accordance with claim 6, wherein said 3D resampling kernel comprises at least one of: a bi-linear kernel, a tri-linear kernel, and a bi-sinc kernel.

8. A method in accordance with claim 1, wherein the step of sampling said surface  $S(\theta, \phi, \varphi, u', v')$  comprises the step of selecting a sub-volume around an origin for resampling, when sampling said surface  $S(\theta, \phi, \varphi, u', v')$  in part c.

9. A method in accordance with claim 1, further comprising padding said sample surface  $S(\theta, \phi, \varphi, u', v')$  with zeros, after sampling said surface  $S(\theta, \phi, \varphi, u', v')$  in part c.

10. A method in accordance with claim 1, further comprising applying a convolution filter to said sample surface  $S(\theta, \phi, \varphi, u', v')$ , by multiplying said sample surface with a 2D fast Fourier Transform of said convolution filter.

11. A method in accordance with claim 1, wherein said 3D scan volume is characterized by spatial dimensions given by  $(M*N*P)$ , and wherein said reconstructed 2D image and said sampling surface are characterized

by spatial dimensions given by (M\*N).

12. A method in accordance with claim 1, wherein said Fourier transform  $F(u,v,w)$  is represented mathematically by:

$$F(u,v,w) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} f(x,y,z) e^{-2\pi j(ux+vy+wz)} dx dy dz.$$

13. A method of generating a 2D DRR (digitally reconstructed radiograph) of a 3D scan volume  $f(x,y,z)$  of an object from 3D scan data representative of said 3D scan volume, for an orientation  $(\theta, \phi, \varphi)$  of said 3D scan volume, the method comprising:

- a. generating a 3D data set in frequency space representative of the 3D Fourier transform  $F(u,v,w)$  of said 3D scan volume  $f(x,y,z)$ ;
- b. resampling said 3D  $F(u,v,w)$  data set along a surface  $S(\theta, \phi, \varphi, u', v')$  within said data set, said surface passing through the origin of said 3D data set and being defined by angles  $(\theta, \phi, \varphi)$  corresponding to said orientation of said 3D scan volume;  
and
- c. computing the 2D inverse Fourier transform  $F^{-1}[S(\theta, \phi, \varphi, u', v')]$  of said surface  $S(\theta, \phi, \varphi, u', v')$  to generate a DRR along a projection direction perpendicular to said surface  $S(\theta, \phi, \varphi, u', v')$ .

14. A method in accordance with claim 13, wherein resampling along said surface  $S(\theta, \phi, \varphi, u', v')$  comprises assigning, to each pixel along said surface in said 3D data set representative of  $F(u,v,w)$ , the value of the closest neighboring pixel.

15. A method in accordance with claim 13, wherein resampling along said surface  $S(\theta, \phi, \varphi, u', v')$  comprises:

- a) selecting a resampling kernel;
- b) for each data point along said surface, multiplying one or more neighboring pixel values with the resampling kernel value at the sample point, and
- c) adding together the multiplied values to form the resampled pixel value.

16. A method in accordance with claim 13, wherein said resampling kernel comprises at least one of:
- a bi-linear resampling kernel;
  - a tri-linear resampling kernel;
  - a sinc resampling kernel; and
  - a bi-sinc resampling kernel.
17. A method in accordance with claim 13, wherein resampling along said surface  $S(\theta, \phi, \varphi, u', v')$  comprises padding said surface with zeros.
18. A method in accordance with claim 13, wherein resampling along said surface  $S(\theta, \phi, \varphi, u', v')$  comprises multiplying said surface with a 2D Fourier transform of a convolution filter.
19. A system for generating a reconstructed 2D image of an object representative of a 3D scan volume  $f(x,y,z)$  of the object, for an orientation  $(\theta, \phi, \varphi)$  of said 3D scan volume, the system comprising:
- a scanner configured to provide 3D scan data representative of said 3D scan volume  $f(x,y,z)$ ;
  - a controller, including:
    - an input module configured to receive said 3D scan data;
    - a first processor configured to generate a 3D data set representative of a 3D Fourier transform  $F(u,v,w)$  of said 3D scan volume  $f(x,y,z)$ , where  $u$ ,  $v$ , and  $w$  represent variables along three mutually orthogonal coordinate axes in the frequency domain;
    - resampling means for resampling said 3D data set along a surface  $S(\theta, \phi, \varphi, u', v')$ , said surface  $S(\theta, \phi, \varphi, u', v')$  being defined at angles  $(\theta, \phi, \varphi)$  corresponding to said orientation of said 3D scan volume; and

iv. a second processor configured to compute a 2D inverse Fourier transform  $F^{-1}[S(\theta, \phi, \varphi, u', v')]$  of said surface  $S(\theta, \phi, \varphi, u', v')$ .

20. A system in accordance with claim 19, wherein said scanner comprises at least one of: a CT scanner; a PET scanner; an MRI scanner; and an ultrasound scanner.

21. A system in accordance with claim 19, wherein said reconstructed 2D image comprises a DRR (digitally reconstructed radiograph).

22. A system in accordance with claim 19, wherein said 2D inverse Fourier transform  $F^{-1}[S(\theta, \phi, \varphi, u', v')]$  is a 2D DRR reconstructed along projection direction that is perpendicular to said surface  $S(\theta, \phi, \varphi, u', v')$ .

23. A system in accordance with claim 22,

wherein said projection direction comprises a direction of a cone projection, the cone projection being the projection of a beam originating from a point source and passing through said scan volume and incident upon a planar 2D surface;

wherein said 2D DRR represents the radiographic image of said scan volume that would be obtained with an imaging beam emitted from a point source disposed at a known position and angle, if said scan volume were positioned in accordance with said 3D scan data; and

wherein said means for sampling said surface  $S(\theta, \phi, \varphi, u', v')$  comprises means for selecting a sampled surface that is part of the surface of a sphere whose center is coincident with said point source.

24. A system in accordance with claim 19, wherein said means for resampling said surface  $S(\theta, \phi, \varphi, u', v')$  comprise means for selecting a 3D resampling kernel.

25. A system in accordance with claim 19, wherein said 3D resampling kernel

comprises at least one of: a bi-linear kernel, a tri-linear kernel, and a bi-sinc kernel.

26. A system in accordance with claim 19, wherein said means for sampling said surface  $S(\theta, \phi, \varphi, u', v')$  comprise means for selecting a sub-volume around an origin for resampling.

27. A system in accordance with claim 19, wherein said 3D scan volume is characterized by spatial dimensions  $(M*N*P)$ , and wherein said reconstructed 2D image and said sampling surface are characterized by spatial dimensions  $(M*N)$ .

28. A system in accordance with claim 19, wherein said resampling means comprise:

- a. means for multiplying, for each data point along said surface, one or more neighboring pixel values with the value of a resampling kernel at said data point; and
- b. means for summing said multiplied values to form a resampled pixel value.

29. A system for generating a DRR of a 3D scan volume  $f(x,y,z)$  of an object, for an orientation  $(\theta, \phi, \varphi)$  of said 3D scan volume, from 3D scan data representative of said volume  $f(x,y,z)$ , the system comprising:

A. a controller, including:

- a. an input module configured to receive said 3D scan data;
- b. a first processor configured to compute a 3D data set in frequency space representative of Fourier transform  $F(u,v,w)$  of said 3D scan volume  $f(x,y,z)$ , where  $u, v$ , and  $w$  represent variables along three mutually orthogonal coordinate axes in the frequency domain;
- c. resampling means for resampling said 3D data set along a surface  $S(\theta, \phi, \varphi, u', v')$ , said surface  $S(\theta, \phi, \varphi, u', v')$  passing through the origin and being defined at angles  $(\theta, \phi, \varphi)$  corresponding to said orientation of said 3D scan volume; and

d. a second processor configured to compute a 2D inverse Fourier transform  $F^{-1} [S(\theta, \phi, \varphi, u', v')]$  of said surface  $S(\theta, \phi, \varphi, u', v')$ ;

wherein said 2D inverse transform  $F^{-1} [S(\theta, \phi, \varphi, u', v')]$  is a DRR along a projection direction perpendicular to said surface  $S(\theta, \phi, \varphi, u', v')$ .